

BIRINCHI TARTIBLI BA'ZI BO'LAKLI O'ZGARMAS ARGUMENTLI  
DIFFERENSIAL TENGLAMA UCHUN UMUMIY YECHIMNI TOPISH ALGORITMI

Raxmanova Charos Tursunboy qizi

Jizzax Davlat Pedagogika Universiteti 2-kurs magistranti

**Annotatsiya.** Hozirgi zamon texnikasining tez rivojlanishi bo'lakli o'zgarmas argumentli birinchi tartibli differensial tenglamalarning yechimlari mavjudligi masalasini qo'yilishi va o'rganilishini talab qilmoqda. Bu mavzu matematika-fizika fani uchun nazariy va amaliy jihatdan katta ahamiyatga egadir.

Shuning uchun ham bo'lakli o'zgarmas argumentli birinchi tartibli differensial tenglamalarning Koshi shartlarida yechimlari mavjudligi mavzusi dolzarb hisoblanadi.

**Kalit so'zlar:** O'zgarmas argument, bo'lakli differensial tenglamada uzluksizlik, differensial tenglamada butun qism

Hozirda tez-tez kuzatiladigan bōlak-bōlak doimiy o'zgarishlar bilan bo'g'liq kōplab hodisalar mavjud. Bōlak-bōlak doimiy tizimlar bu hodisalarni bōlak-bōlak doimiy argumentni o'z ichiga olgan tegishli differensial tenglamalar bilan modellashtirilishi mumkin. Ushbu nazariya 1-marta K.Kuk va boshqalar tomonidan o'rganilgan. Ushbu differensial tenglamada doimiy argument ma'lum oraliqlarda doimiy bōlgan argumentlarni o'z ichiga oladi(masalan, eng katta butun funksiya) Maqolada bo'laklangan doimiy bōlgan chiziqli bōlmagan impulsiv differensial tenglamaning tebranishlari kōrib chiqildi. Impulsiv chiziqli bōlmagan 1-tartibli differensial tenglamalar sinfi yechimlarining mavjudligi va o'ziga xosligiga e'tibor qaratdi va bōlak-bōlak doimiy argumentlarga ega tebranishlar uchun yetarli sharoitlarni tahlil qilinadi.

1-qadam.  $x'(t) = x(t)g(x([t]))$ ,  $t \in [0, \infty)$ ,  $x(0) = c_0$  tenglamani  $[0,1)$  oraliqda integrallaymiz:

$$x(t) = c_0 e^{g(x(0))t}, \quad x(0) = c_0.$$

2-qadam. Uzluksiz xossasiga ko'ra

$$x(1) = \lim_{t \rightarrow 1-0} x(t) = c_0 e^{g(x(0))}$$

3-qadam.  $x'(t) = x(t)g(x([t]))$ ,  $t \in [0, \infty)$ ,  $x(1) = c_1$  tenglamani  $[1,2)$  oraliqda integrallaymiz:

$$x(t) = c_1 e^{g(x(1))(t-1)}, \quad x(1) = c_1$$

4-qadam.

$$x(1) = \lim_{t \rightarrow 1-0} x(t) = c_0 e^{g(x(0))}$$

Tenglikdan foydalanib,  $x(t) = c_0 e^{g(x(0))} e^{g(c_0 e^{g(x(0))})(t-1)}$ ,  $[1,2)$  oraliqda.

5-qadam. Uzluksizlik xossasiga ko'ra

$$x(2) = \lim_{t \rightarrow 2-0} x(t) = c_0 e^{g(x(0))} e^{g(c_0 e^{g(x(0))})},$$

6-qadam.  $x'(t) = x(t)g(x([t]))$ ,  $t \in [0, \infty)$ ,  $x(k) = c_k$  tenglamani  $[k, k + 1)$  oraliqda

$$x(t) = c_k e^{g(x(k))(t-k)},$$

7-qadam. Uzluksizlik xossasiga ko'ra

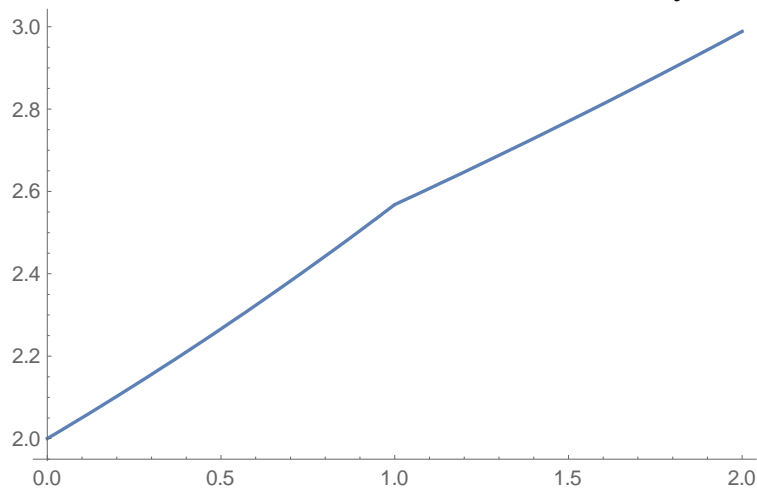
$$x(k) = \lim_{t \rightarrow k-0} x(t) = c_0 e^{g(x(0))} e^{g(c_0 e^{g(x(0))})} \dots$$

Misol-3.1.

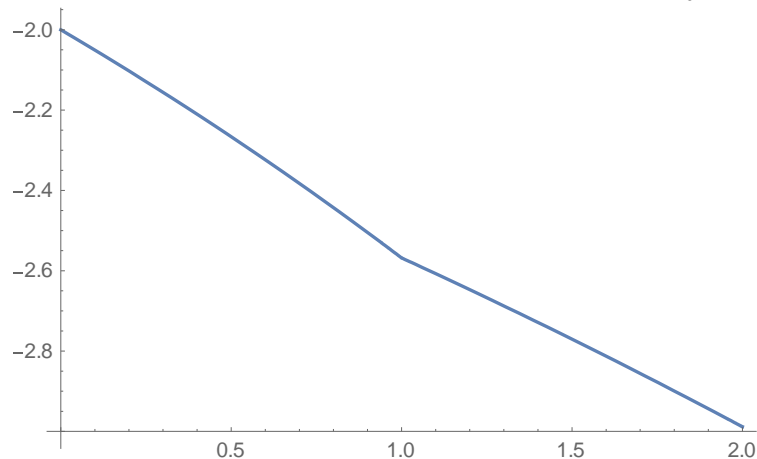
$x'(t) = x(t)g(x([t]))$ ,  $t \in [0, \infty)$ ,  $x(0) = c_0$  masalani  $[0, 2)$  orliqda yechimini topamiz:

$$x(t) = \begin{cases} c_0 e^{g(c_0)t}, & t \in [0, 1), \\ c_0 e^{g(c_0)} e^{g(c_0 e^{g(c_0)})(t-1)}, & t \in [1, 2). \end{cases}$$

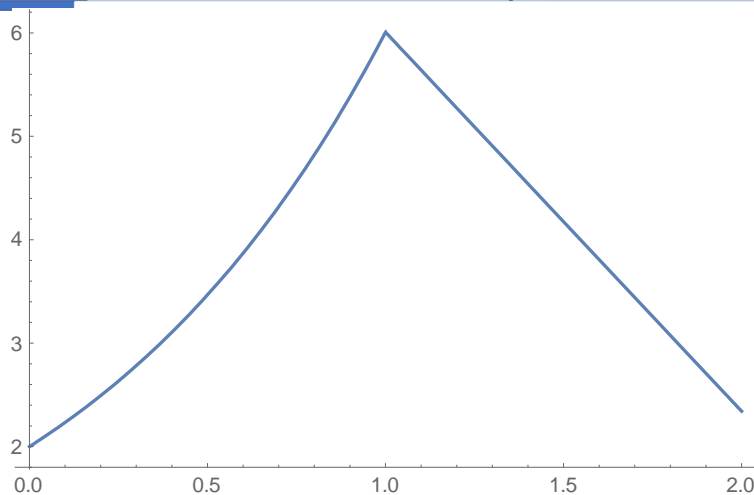
a) Agar  $c_0 = 2$  va  $g(t) = \frac{1}{t^2}$  bo'lsa,



b) Agar  $c_0 = -2$  va  $g(t) = \frac{1}{t^2}$  bo'lsa,



c) Agar  $c_0 = 2$  va  $g(t) = \frac{1}{\sin t}$  bo'lsa,



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